

The Network Foundations of Credit Counterparty Risk: Theory and Evidence*

Jonathan Brogaard[†]

Belinda (Chen) Chen[‡]

Abstract

We develop a structural model of credit counterparty risk in which contagion arises from an inter-firm production network. We then propose a parsimonious empirical approach that directly incorporates network topology to predict credit spreads. We find that incorporating network edge features induces an average credit-spread change of approximately 21.8% and yields an incremental R^2 of 0.56 in explaining credit spreads. Our results show that network-based counterparty risk is strongly priced and plays a first-order role in shaping credit spreads, particularly during periods when production networks experience severe disruption, reorganization, or rewiring. Network effects are especially important for firms operating in industries that occupy intermediate positions within supply chains, rely heavily on distribution and logistics, and face low substitutability of inputs.

Keywords: Credit Risk, Counterparty Risk, Production Network, Idiosyncratic Risk Spillover

JEL Classification: C45, C58, G12, G17

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[†]David Eccles School of Business, University of Utah; brogaardj@eccles.utah.edu

[‡]Shanghai Advanced Institute of Finance (SAIF), Shanghai Jiao Tong University; chenchen@saif.sjtu.edu.cn

1 Introduction

The interdependence of firms’ default intensities constitutes a central topic in the study of credit risk. A large body of literature documents that default clustering arises for multiple reasons. First, firms are exposed to common shocks or correlated risk factors (e.g., [Duffie and Singleton \(1999\)](#), [Collin-Dufresne, Goldstein, and Martin \(2001\)](#), and [Duffie and Gârleanu \(2001\)](#)), so that default probabilities are jointly driven by aggregate macroeconomic conditions. Second, firms may experience firm-specific (idiosyncratic) shocks that propagate to other firms due to economic linkages, giving rise to contagion through firm networks.

Empirical studies such as [Das, Duffie, Kapadia, and Saita \(2007\)](#) and [Jorion and Zhang \(2009\)](#) provide strong evidence that idiosyncratic risk contagion—often referred to as counterparty risk—can explain excess default clustering beyond what is attributable to common risk factors alone. In addition, a growing theoretical literature (e.g., [Jarrow and Yu \(2001\)](#), [Jorion and Zhang \(2007\)](#), and [Azizpour, Giesecke, and Schwenkler \(2018\)](#)) has developed structural frameworks that incorporate counterparty risk into models of default intensities and credit spreads. However, due to substantial analytical and estimation complexity, most existing models are tractable only under highly simplified settings, such as two-firm economies or assumptions that rule out cascading or looping effects—that is, situations in which a firm-specific shock propagates through multiple firms and potentially feeds back into the originating firm before spreading further through the network.

In this paper, we study a general credit risk framework with the following features: (i) n firms are economically linked through a network structure; (ii) cascade effects are permitted; (iii) contagion is asymmetric across firms; and (iv) ordinary idiosyncratic shocks—rather than only extreme firm-specific tail events—can propagate through the network. Our analysis focuses on the implications of the inter-firm network structure for the cross-sectional behavior of credit spreads.

Unlike much of the existing literature in which economic linkages are left unspecified, we explicitly model inter-firm connections as production-based input–output relationships. This discipline allows us to provide a granular network-based interpretation of counterparty risk, clarifying how both the global structure of the network and a firm’s position within it shape the propagation of idiosyncratic default risk. In practice, firms are connected through multiple channels, including production networks, cross-holdings of assets, debt and liability exposures, and other contractual relationships, all of which may facilitate idiosyncratic risk spillovers. We focus on the production network as the primary channel because there is substantial

empirical evidence that real default contagion occurs along supplier–customer chains (e.g., [Jacobson and Von Schedvin \(2015\)](#)). While we do not rule out alternative transmission mechanisms, our framework emphasizes the production network to deliver a clear and economically grounded mechanism. Once this channel is well understood, the analysis can be readily extended to incorporate other forms of inter-firm linkages. Finally, our framework does not rely on specific time-series assumptions about default intensities.¹ Instead, our primary contribution lies in characterizing how the cross-sectional $n \times n$ network structure governs the propagation of idiosyncratic default risk.

Theoretically, we develop a structural framework in which each firm’s default intensity depends on a macroeconomic variable M , firm-specific characteristics X_i , and counterparty risk components a_{ij} , where a_{ij} captures idiosyncratic default-risk spillovers from firm j to firm i through the production input-output network. We provide an economic interpretation of a_{ij} by building on the key insights of [Herskovic \(2018\)](#) and [Chen \(2023\)](#). Specifically, both studies develop a production-based general equilibrium model with n representative firms that links real production to firms’ investment decisions. In this framework, each firm produces a single good that is used as an intermediate input by other firms, and firms use sales revenue—that is, cash flows—to issue equity held by households. Firms are subject to i.i.d. idiosyncratic productivity shocks, which affect their own final output and subsequently spill over to downstream firms by affecting input supplies, cash flows, and stock returns.²

Motivated by this result, we define an $n \times n$ adjacency matrix $A \equiv [a_{ij}]$ to characterize the structure of *idiosyncratic* risk spillovers arising from the production network. As a model implication, each element a_{ij} is an endogenous function of the underlying production network weights. A larger value of a_{ij} indicates that firm j exerts a stronger idiosyncratic risk propagation effect on firm i . This effect reflects the overall importance of firm j to firm i through three channels: (i) the direct importance of firm j ’s output as an input supplier to firm i ; (ii) the indirect importance of firm j ’s output through other firms in the production network that subsequently affect firm i ; and (iii) the importance of firm j ’s output for aggregate household consumption, which in turn feeds back to firm i .

When a_{ij} is large, firm j constitutes an economically important supplier to firm i , capturing both direct and indirect input linkages. A negative idiosyncratic shock to firm j reduces its output and disrupts firm i ’s

¹[Das et al. \(2007\)](#) adopt a similar modeling strategy.

²While both [Herskovic \(2018\)](#) and [Chen \(2023\)](#) do not distinguish between positive and negative idiosyncratic productivity shocks, we focus on the propagation of *negative idiosyncratic shocks* and interpret these spillovers specifically in terms of default risk.

effective input supply. This disruption lowers firm i 's expected cash flows and equity value, while increasing the volatility of cash flows and, consequently, equity return volatility.

We link this channel to firm i 's default intensity by adopting a distance-to-default (DD) framework following [Bharath and Shumway \(2008\)](#). In this framework, the original Merton DD model is simplified in a computationally tractable manner, allowing all components to be approximated using observable market data. Specifically, a firm's distance to default depends on the deviation of the market value of equity from the face value of debt, scaled by the volatility of firm asset value (the combined value of debt and equity), where asset volatility can be approximated as a linear function of equity volatility.

Under the assumption of a constant interest rate and fixed debt face value and maturity, a decline in firm i 's equity value and an increase in firm i 's equity volatility both reduce its distance to default. A lower distance to default, in turn, implies a higher default probability and default intensity. Consequently, a larger a_{ij} increases firm i 's default intensity through the cash-flow news channel operating via the input-output linkage.

After expressing firm i 's default intensity as a structural function that depends positively on the network components a_{ij} , we derive the credit default swap (CDS) spread for firm i under the risk-neutral measure. The CDS spread is determined by equating the expected present value of premium payments to the expected present value of default loss payments. The analytical solution implies that firm i 's CDS spread depends on a *nonlinear* function of macroeconomic conditions, firm-specific characteristics, and production-network spillover terms a_{ij} for all j , with the partial derivative $\frac{\partial \text{CDS}_i}{\partial a_{ij}} > 0$. This result implies that credit spreads are best explained by incorporating the production-network structure $\{a_{ij}\}$ in a nonlinear manner.

We next provide empirical evidence to support the structural framework. There are two natural approaches, both of which face significant obstacles. First, directly estimating the fully specified structural model is computationally infeasible in large production networks. Existing structural counterparty-risk models, such as [Jarrow and Yu \(2001\)](#), are tractable only under highly simplified assumptions—for example, two-firm economies without cascading network effects. Second, directly applying statistical prediction methods, including standard machine-learning algorithms, faces a fundamental limitation relative to our structural framework: these approaches typically rely on firm-level features as inputs, but cannot directly incorporate the full network topology—represented by an $n \times n$ adjacency matrix—as a predictive object.

To address these challenges, we adopt a recently developed machine-learning methodology: graph neural networks (GNNs). GNNs are explicitly designed to capture global graph topology and to model data

with complex cross-sectional dependence, making them a natural empirical counterpart to our production-network-based structural framework.

Unlike much of the machine-learning literature, which emphasizes extensive model tuning and increasingly sophisticated architectures to maximize pooled out-of-sample predictive performance, our objective is different. We deliberately employ a parsimonious GNN architecture that is sufficient to deliver clear financial interpretation of network effects. In doing so, we sacrifice architectural complexity in favor of economic transparency. Our empirical analysis pursues two primary objectives: (i) to assess the incremental predictive power of production-network information for credit spreads relative to non-network benchmarks, and (ii) to characterize which firms' credit spreads are most exposed to counterparty risk through the network and the economic states in which such network risk is most strongly priced.

In our GNN framework, each firm is represented as a node, and each firm-to-firm idiosyncratic risk spillover is represented as a weighted, directed edge. The model incorporates both node-level features—such as firm-specific characteristics and macroeconomic variables—and edge-level features, which capture the magnitude of production-network spillovers a_{ij} . These spillover measures are estimated using input–output data and stock return data following [Diebold and Yilmaz \(2014\)](#) and [Chen \(2023\)](#). The GNN aggregates information from neighboring nodes and edges to construct firm-level latent representations, which are then used to predict CDS spreads.

We evaluate the empirical results in light of the two objectives above by conducting the following analyses. First, we compare the out-of-sample performance of the GNN model with a set of nonlinear benchmark models that rely on the same node-level features but exclude network information. Among these benchmarks, the convolutional neural network (CNN) provides a natural point of comparison. We design the CNN architecture under strict assumptions so that it corresponds to a GNN in which all network edges are set to zero.

Under identical training and validation protocols, we find that the GNN substantially reduces out-of-sample prediction error, with the RMSE declining to 0.89, compared with 1.34 for the CNN benchmark. Economically, we find that incorporating network edge features induces an average spread change of approximately 21.8% in the full sample and yields an incremental R^2 of 0.56 in explaining credit spreads. This result corroborates the central role of network effects in the structural model.

The improvement in predictive accuracy is present for both investment-grade and high-yield firms, with a more pronounced effect for investment-grade firms. Intuitively, investment-grade firms are typically

large, mature, and highly interconnected through multiple input–output relationships, which places them in more central positions within production networks. As a result, incorporating network characteristics is particularly informative for predicting the CDS spreads of investment-grade firms, whose credit risk is more exposed to contagion through complex production linkages.

Second, we assess the time-varying importance of network structure by examining out-of-sample prediction performance at a monthly frequency. The resulting time-series evidence reveals that GNN models consistently outperform all competing approaches throughout the sample. In several periods, the RMSE achieved by GNNs is as low as one quarter of that produced by alternative algorithms, particularly relative to dimension-reduction methods such as PCR and PLS. This persistent performance gap indicates that pairwise inter-firm network information captures a substantial component of credit risk that is not explained by firm-level characteristics alone.

Moreover, we find there are several episodes in which network structure becomes especially important. The first occurs during the 2008 financial crisis. During severe economic downturns, production networks are disrupted as firms face liquidity constraints and operational distress. Under such conditions, inter-firm contagion and counterparty risk become first-order determinants of credit spreads, which GNNs are well equipped to capture.

A second episode occurs in late 2009 and early 2010, when equity prices rebounded sharply and firms began repairing previously disrupted production linkages. This transition period involved substantial uncertainty due to portfolio reallocation and network reconfiguration. Models that ignore network structure experience sharp increases in RMSE, whereas GNNs maintain strong predictive performance by accounting for evolving inter-firm dependencies.

A third episode occurs around 2018, coinciding with the escalation of trade tensions and tariff policies. Tariffs can be viewed as disruptions to trade linkages that increase fragility in global value chains. During this period, CDS spreads reflect firms' exposure to affected trade partners, again amplifying the role of network structure.

Finally, following the onset of the COVID-19 pandemic in 2020, widespread production shutdowns—such as factory closures in the semiconductor sector—generated severe upstream supply disruptions. Downstream firms reliant on these inputs experienced heightened fragility, leading to pronounced network-driven credit risk. GNNs capture these cascading effects, while non-network models fail to do so.

The time-series evidence suggests that the full inter-firm network captures an important component of

systematic risk that is priced in CDS spreads. These findings echo the production network literature (e.g., [Acemoglu, Carvalho, Ozdaglar, and Tahbaz-Salehi, 2012](#)), which emphasizes that network structure provides a microfoundation for systematic risk.

In addition, we examine the network-attributable credit spread change across sectors to identify which industries' credit spreads are more susceptible to supply-chain disruptions.

We find that network features tend to matter more for firms that (i) occupy intermediate positions in the production chain and are exposed to both upstream and downstream risks, (ii) rely heavily on shipping, logistics, and distribution across the supply chain, or (iii) depend on specialized inputs that are difficult to substitute. For such firms, disruptions or shocks propagating through supplier–customer relationships can lead to substantial changes in expected cash flows and, consequently, credit spreads. Industries exhibiting these characteristics include electrical equipment, shipbuilding, railroad equipment, and defense. For example, we find that network features induce especially large spread changes for the defense sector during the period from 2014 to 2018, which coincides with discrete geopolitical shocks such as the Russia–Ukraine conflict and conflicts involving ISIS. During such periods, defense demand becomes lumpy and state-dependent, and contracts may be renegotiated, accelerated, delayed, or repriced.

By contrast, industries whose credit risk is primarily driven by firm-specific fundamentals or final demand exhibit smaller network-attributable spread changes. For instance, network edge features induce relatively modest shifts in the credit spreads of natural resource extraction industries (mining and coal), which are heavily influenced by commodity prices and balance-sheet leverage. Similarly, the entertainment and textile sectors rely more heavily on idiosyncratic fundamentals such as intellectual property, brand value, and consumer sentiment, and often operate with more diversified supplier and customer bases. As a result, changes in supply-chain networks play a more limited role in shaping their credit spreads.

Related Literature

This paper contributes to the literature on credit risk. A large body of work proposes structural models to study default clustering, credit risk spillovers, and interconnectedness in credit markets. Default clustering is commonly attributed to two broad mechanisms. First, firms may be exposed to common risk factors, which are typically modeled through state variables or aggregate macroeconomic shocks (e.g., [Collin-Dufresne, Goldstein, and Martin \(2001\)](#), [Duffie and Gârleanu \(2001\)](#)). Second, default clustering may arise from firm-specific shocks—namely, idiosyncratic risks—that propagate through economic linkages. Related studies

include [Jarrow and Yu \(2001\)](#), [Das et al. \(2007\)](#), [Jorion and Zhang \(2007\)](#), [Jorion and Zhang \(2009\)](#), and [Azizpour, Giesecke, and Schwenkler \(2018\)](#). Our paper primarily contributes to the second strand of the literature by studying idiosyncratic default-risk contagion through inter-firm networks. To our knowledge, this is the first paper to provide a comprehensive framework for understanding how the entire network structure shapes credit risk. While most existing structural models focus on highly simplified settings—such as two-firm economies, the absence of cascading effects, and contagion driven only by extreme firm-specific tail events—and typically do not explicitly specify the underlying economic linkages, we develop a more general credit risk structural model with the following features: (i) n firms are economically linked through a network structure that is explicitly identified as a production-based input–output network; (ii) cascade effects are permitted; (iii) contagion is asymmetric across firms; and (iv) ordinary idiosyncratic shocks, rather than only tail events, can propagate through the network. We focus on examining how inter-firm network structure and firms’ positions within the network shape the cross-sectional behavior of credit spreads.³ While some CDS-focused studies (e.g., [Getmansky, Girardi, and Lewis \(2016\)](#)) emphasize counterparty risk arising from common protection sellers such as dealers, our analysis abstracts from dealer cores and OTC market structure. Instead, we focus on inter-firm economic connections operating through production networks.

Beyond the counterparty-risk literature, there is a broad body of research on modeling and measuring credit and default risk, including [Merton \(1974\)](#), [Duffie and Singleton \(1999\)](#), [Duffie \(1999\)](#), [Duffie, Pan, and Singleton \(2000\)](#), [Duffie and Lando \(2001\)](#), [Duffie and Pan \(1997\)](#), [Duffie, Pedersen, and Singleton \(2003\)](#), [Duffie, Saita, and Wang \(2007\)](#), [Bharath and Shumway \(2008\)](#), [Bao and Pan \(2013\)](#), and [Hu, Pan, and Wang \(2013\)](#). We contribute to this literature by explicitly incorporating counterparty risk through inter-firm networks into a structural credit risk framework.⁴ Some papers (e.g., [Giesecke, Longstaff, Schaefer, and Strebulaev \(2011\)](#)) emphasize the presence of a non-default-related credit risk premium. From a structural perspective, this premium compensates investors for exposure to adverse states that do not necessarily involve realized default. Such premia are particularly important during recessions, when bond prices decline sharply, and are often modeled through time-varying volatility, differences between physical and risk-neutral default probabilities, or rare-disaster risk. In contrast, our paper focuses on a parsimonious framework that does not

³Related contributions include [Hawkes \(1971\)](#), [Giesecke \(2002\)](#), [Giesecke and Weber \(2004\)](#), [Giesecke \(2004\)](#), [Kitwittanachai and Pearson \(2015\)](#), [Benzoni, Collin-Dufresne, Goldstein, and Helwege \(2015\)](#), [Aït-Sahalia, Cacho-Diaz, and Laeven \(2015\)](#), and [Jacobson and Von Schedvin \(2015\)](#).

⁴Additional related studies include [Altman \(1968\)](#), [Duffie and Liu \(2001\)](#), [Almeida and Philippon \(2007\)](#), [Campbell, Hilscher, and Szilagyi \(2008\)](#), [Longstaff, Pan, Pedersen, and Singleton \(2011\)](#), [Ang and Longstaff \(2013\)](#), [Gouriéroux, Monfort, and Renne \(2014\)](#), [Galil, Shapir, Amiram, and Ben-Zion \(2014\)](#), [Kitwittanachai \(2015\)](#), [Berndt, Douglas, Duffie, and Ferguson \(2018\)](#), [Boyarchenko and Shachar \(2020\)](#), [Monfort, Pegoraro, Renne, and Roussellet \(2021\)](#), and [Bao, Hou, and Zhang \(2023\)](#).

rely on specific time-series assumptions about default intensities—an approach also adopted by [Das et al. \(2007\)](#). Instead, we emphasize how the cross-sectional $n \times n$ network structure governs the propagation of default risk.

Our work also contributes to the growing literature on inter-firm networks, particularly production-based networks. A large body of research develops production-based multisector models to study the implications of network structure for aggregate productivity, aggregate volatility, and macroeconomic tail risk (e.g., [Carvalho \(2008\)](#), [Acemoglu et al. \(2012\)](#), [Carvalho and Gabaix \(2013\)](#), [Herskovic \(2018\)](#), and [Chen \(2023\)](#)). We adapt this production-based input–output framework to provide an economically grounded explanation for the existence of counterparty risk and to offer a comprehensive analysis of the role of production networks in shaping credit spreads.⁵

Finally, this paper contributes to the growing literature on machine learning in finance. A number of studies, including [Kelly, Pruitt, and Su \(2019\)](#), [Gu, Kelly, and Xiu \(2020\)](#), and [Gu, Kelly, and Xiu \(2021\)](#), apply machine-learning techniques to asset pricing and return prediction, demonstrating their effectiveness in handling high-dimensional data. Our paper introduces graph neural networks (GNNs) as a novel empirical tool for integrating granular and global network-topology information to explain credit spreads.⁶

The remainder of the paper is organized as follows. Section 2 outlines a conceptual framework for CDS pricing. Section 3 presents the empirical evidence. Section 4 concludes.

2 Structural Framework

2.1 Production-Network Exposure

We consider a production-based multi-firm network model developed in [Herskovic \(2018\)](#) and [Chen \(2023\)](#), which links real production to firms’ investment and asset prices. While these frameworks abstract from leverage and default, we extend the setting by allowing firms to issue defaultable debt in the form of a zero-coupon bond.

We study a production economy with n firms indexed by $i = 1, \dots, n$. Each firm purchases other firms’

⁵Additional related literature includes [Gabaix \(2011\)](#), [Diebold and Yilmaz \(2014\)](#), [Acemoglu, Akcigit, and Kerr \(2016\)](#), [Blasques, Koopman, Lucas, and Schaumburg \(2016\)](#), [Härdle, Wang, and Yu \(2016\)](#), [Acemoglu, Ozdaglar, and Tahbaz-Salehi \(2017\)](#), [Demirer, Diebold, Liu, and Yilmaz \(2018\)](#), [Chen, Härdle, and Okhrin \(2019\)](#), [Liu \(2022\)](#), [Dew-Becker \(2023\)](#), [Engle and Kelly \(2012\)](#), [Herskovic, Kelly, Lustig, and Van Nieuwerburgh \(2016\)](#), and [Herskovic, Kelly, Lustig, and Van Nieuwerburgh \(2020\)](#).

⁶Additional related work includes [Kelly and Jiang \(2014\)](#), [Kelly, Malamud, and Zhou \(2024\)](#), [Wang, Lin, Cui, Jia, Wang, Fang, Yu, Zhou, Yang, and Qi \(2019\)](#), [Uddin, Tao, and Yu \(2021\)](#), and [Zhang, Pu, Cucuringu, and Dong \(2023\)](#).

goods as intermediate inputs in order to produce its own output. A firm's output can either be used as an intermediate input by other firms or be directly consumed by the representative household. Each firm's production technology is subject to negative idiosyncratic productivity shocks.

Firms use the cash flows generated from selling their real output to issue equity, which is held by the household. As a result, idiosyncratic productivity shocks propagate through the supply chain and affect firms' cash flows, dividends, and stock returns. In addition, each firm i issues a single zero-coupon bond with face value F_i and maturity T . The risk-free interest rate r is constant, and the face value F_i is fixed and does not vary with economic conditions.

As shown in [Chen \(2023\)](#), the production network generates rich cross-firm dependencies not only in cash flows, dividends, stock returns, and return volatilities, but also in idiosyncratic return volatilities—that is, the volatility of residual returns after removing common components. Importantly, this idiosyncratic volatility spillover structure provides a natural measure of pairwise systemic risk within the production network. In this paper, we focus on this pairwise systemic risk measure and explore its implications for credit spreads. Specifically, we define an $n \times n$ adjacency matrix,

$$A \equiv [a_{ij}]_{i,j=1}^n, \quad (1)$$

which characterizes pairwise idiosyncratic risk spillovers across firms as summarized by equation (1). We take this structural result as the starting point of our analysis and leave the detailed derivation of the full production equilibrium to the Internet Appendix.

As a model implication, each element a_{ij} in equation (1) is an endogenous function of the underlying production network weights. A larger value of a_{ij} indicates that firm j exerts a stronger idiosyncratic risk propagation effect on firm i . This effect reflects the overall importance of firm j to firm i through three channels: (i) the direct importance of firm j 's output as an input supplier to firm i ; (ii) the indirect importance of firm j 's output through other firms in the production network that subsequently affect firm i ; and (iii) the importance of firm j 's output for aggregate household consumption, which in turn feeds back to firm i .

Let $u_{j,t} \geq 0$ denote a negative idiosyncratic productivity shock to firm j at time t . Firm i 's operating cash-flow innovation is given by

$$\Delta\pi_{i,t} = \beta'_M M_t + \beta'_X X_{i,t} - \sum_{j=1}^n a_{ij} u_{j,t}, \quad (2)$$

as shown in equation (2), where M_t is a vector of aggregate macroeconomic conditions and $X_{i,t}$ is a vector of firm-specific characteristics.

Negative supplier shocks reduce firm i 's expected cash flows in proportion to its downstream exposure a_{ij} in equation (2). In addition, supplier disruptions increase uncertainty in downstream production. We therefore allow cash-flow volatility to depend on production-network exposure according to

$$\text{Var}_t(\Delta\pi_{i,t}) \equiv \sigma_{\pi,i,t}^2 = \bar{\sigma}_{\pi,i}^2 + \sum_{j=1}^n a_{ij}^2 \sigma_{u,j,t}^2, \quad (3)$$

as specified in equation (3), where $\bar{\sigma}_{\pi,i}^2$ is a firm-specific baseline variance and $\sigma_{u,j,t}^2$ denotes the conditional variance of supplier j 's downside shock.

2.2 Capital Structure and Distance to Default

Let $V_{i,t}$ denote the market value of firm i 's assets at time t , defined as the present value of future operating cash flows. Equity holders have limited liability, so the market value of equity satisfies

$$E_{i,t} = \max(V_{i,t} - F_i e^{-r(T-t)}, 0), \quad (4)$$

as given in equation (4).

Following the distance-to-default framework of [Bharath and Shumway \(2008\)](#), distance to default for firm i at time t is defined as

$$DD_{i,t} = \frac{\ln\left(\frac{V_{i,t}}{F_i}\right) + \left(r - \frac{1}{2}\sigma_{V,i,t}^2\right)(T-t)}{\sigma_{V,i,t}\sqrt{T-t}}, \quad (5)$$

as shown in equation (5), where $\sigma_{V,i,t}$ denotes the volatility of firm asset value.

Consistent with [Bharath and Shumway \(2008\)](#), asset value and asset volatility are approximated using observable equity market data according to

$$V_{i,t} \approx E_{i,t} + F_i, \quad (6)$$

$$\sigma_{V,i,t} \approx \frac{E_{i,t}}{V_{i,t}} \sigma_{E,i,t}, \quad (7)$$

as specified in equations (6) and (7), where $\sigma_{E,i,t}$ denotes equity return volatility.

We allow equity value and equity volatility to depend on production-network exposure as follows:

$$\ln E_{i,t} = \alpha_i + \alpha'_M M_t + \alpha'_X X_{i,t} - \sum_{j=1}^n a_{ij} \theta_{j,t} + \eta_{i,t}, \quad (8)$$

$$\sigma_{E,i,t} = \bar{\sigma}_{E,i} + \sum_{j=1}^n a_{ij} \phi_{j,t}, \quad (9)$$

as described in equations (8) and (9), where $\theta_{j,t} \geq 0$ captures supplier-specific downside cash-flow news and $\phi_{j,t} \geq 0$ captures supplier-specific downside uncertainty.

2.3 Default Probability and Credit Spreads

To price credit default swaps, we approximate the risk-neutral default probability over the CDS horizon $[t, T]$ as

$$\mathbb{P}_{i,t}^{\mathbb{Q}}(\text{default by } T) \approx \Phi(-DD_{i,t}), \quad (10)$$

as given in equation (10), abstracting from time variation in risk premia.

Assuming fractional recovery of par $R \in (0, 1)$ and a zero-coupon approximation for the CDS contract, the par CDS spread $s_{i,t}$ satisfies

$$s_{i,t} = (1 - R) \frac{\mathbb{P}_{i,t}^{\mathbb{Q}}(\text{default by } T)}{T - t}, \quad (11)$$

as defined in equation (11).

Substituting equation (10) into equation (11) yields the simplified CDS spread,

$$s_{i,t} = \frac{1 - R}{T - t} \Phi(-DD_{i,t}), \quad (12)$$

as shown in equation (12).

Equations (1)–(12) jointly imply that firm i 's CDS spread is a nonlinear function of macroeconomic conditions, firm-specific characteristics, and production-network exposure $\{a_{ij}\}_{j=1}^n$. In particular, greater downstream exposure to negative supplier shocks lowers distance to default and increases credit spreads.

3 Empirical Evidence

We provide empirical support for our structural framework, which emphasizes the importance of the entire network topology in explaining credit spreads. To this end, we adopt a recently developed machine-learning methodology—graph neural networks (GNNs)—to conduct CDS spread prediction exercises. GNNs are specifically designed to model data with complex cross-sectional dependence and to incorporate rich network topology features as inputs, making them a natural empirical counterpart to our structural framework.

The basic intuition behind the GNN architecture is to represent the inter-firm network explicitly. Each firm is modeled as a node, while each firm-to-firm idiosyncratic risk spillover measure is represented as a weighted and directed edge. The model takes both node-level features—such as firm-specific characteristics and macroeconomic variables—and edge-level features, namely the idiosyncratic risk spillover measures a_{ij} , as inputs. Through a sequence of message-passing and aggregation steps, the GNN embeds information from the network structure and edge weights into latent node-level representations, which are then used to predict CDS spreads in a standard neural network framework.

We briefly describe the GNN architecture below and relegate architecture details to the Internet Appendix. We then describe the data construction, with particular emphasis on the measurement of node-level and edge-level features, and finally present the CDS spread prediction results.

3.1 Architecture of the Empirical Algorithm

In much of the machine-learning literature, researchers emphasize extensive model tuning and increasingly sophisticated architectures to maximize out-of-sample predictive performance. Our objective and approach differ. We deliberately employ a parsimonious vanilla GNN architecture that is sufficient to deliver a clear financial interpretation of network effects.

The Graph Neural Network (GNN) framework consists of two key components: an inter-layer message-passing scheme and an intra-layer updating scheme, with the latter corresponding to the standard updating mechanism used in conventional neural network architectures such as CNNs.

Figure 1 illustrates the inter-layer message-passing scheme that is specific to GNNs.

FIGURE 1 ABOUT HERE

This scheme determines how initial node-level and edge-level features are transformed into latent node representations. Specifically, each normalized embedding $\hat{h}_i^{(k)}$ at layer k incorporates information from node i and its neighbors according to

$$\hat{h}_i^{(k)} = h_i^{(k)} \bigoplus_{j \in \mathcal{N}(i)} (a_{ij}), \quad (13)$$

where $\hat{h}_i^{(k)}$ denotes the normalized embedding of node i at layer k , $h_i^{(k)}$ is the embedding of node i at layer k , \bigoplus represents the concatenation operator, and $\mathcal{N}(i)$ denotes the neighborhood of node i .

In equation (17), a_{ij} represents the directed idiosyncratic risk spillover from node j to node i . Collecting all a_{ij} yields the adjacency matrix $A \equiv [a_{ij}]$. To encode network effects, we follow the graph convolutional network (GCN) formulation of Kipf and Welling (2016). Under this framework, network information is incorporated as

$$\hat{H}^{(k)} = D^{-1} \hat{A} H^{(k)} W^{(k)}, \quad \text{if } A \text{ is asymmetric,} \quad (14)$$

where $\hat{H}^{(k)}$ is the output of the k -th layer, $\hat{A} = A + I$ with I denoting the identity matrix, D is the out-degree matrix, $H^{(k)}$ is the input to the k -th layer, and $W^{(k)}$ is the trainable weight matrix. The out-degree matrix D is diagonal, with diagonal elements equal to the column sums of A .

The intuition is as follows. Each row of the adjacency matrix $A = [a_{ij}]$ reflects the extent to which firm i receives idiosyncratic risk spillovers from other firms. By multiplying this row by neighboring firms' features and aggregating the results, the model assigns greater weight to more economically important suppliers. After aggregating weighted supplier information together with firm i 's own characteristics, the GNN constructs a latent representation of firm i . The matrix D^{-1} serves to normalize the adjacency matrix. Thus, the contribution of neighboring information depends on the economic importance of the supplier to firm i .

The intra-layer updating scheme governs how node representations are transformed from one hidden layer to the next. This structure is standard across neural network architectures. Each layer applies a sequence of operations to the node representations, including batch normalization, dropout, nonlinear activation (ReLU), and an aggregation function. In standard neural networks, the aggregation function typically takes the form of an equally weighted average. In GNNs, however, aggregation is performed by combining neighboring

node characteristics using edge-weighted averages, thereby reflecting the relative importance of neighboring information.

The architecture described above corresponds to the vanilla GNN baseline, which is fundamentally cross-sectional. That is, it operates on a single cross-sectional network snapshot to predict outcomes in the subsequent period. Unlike CNNs, which naturally incorporate temporal pooling, the vanilla GNN does not include an explicit mechanism for temporal aggregation. Although we implement an extended architecture with pooling over time in the Internet Appendix, we focus on the baseline specification in the main analysis. This choice is beneficial for two reasons. First, it is consistent with our structural framework, which emphasizes cross-sectional network effects rather than explicit dynamic propagation. Second, introducing temporal pooling requires additional assumptions—such as recurrent structures (e.g., LSTM)—that increase model complexity and reduce interpretability. Moreover, CDS data are sparse and unevenly observed across firms and time, which necessitates masking schemes that further obscure economic interpretation. Therefore, we focus on the vanilla structure in the main analysis.

3.2 Data and Implementation Details

We use daily Markit CDS data for U.S. firms spanning January 2005 to December 2020.⁷ We focus on the 5-year tenor and senior unsecured contracts, which are the most liquid in the CDS market. We use spreads from the prevalent XR14 contract. The spread on XR contracts reflects default risk while excluding restructuring risk, which aligns with our structural framework.⁸

We construct a monthly panel by retaining the most recent CDS spread observed in each month. The final dataset contains 678 firms and 130,176 firm-month observations over the sample period.

TABLE 1 AND FIGURE 3 ABOUT HERE

Table 1 reports summary statistics for the distribution of log CDS spreads, along with firms' market capitalization and implied credit ratings. Columns 1–2 show that CDS contracts are observed for a median duration of 137 months (11.4 years), with a minimum of 2 months and a maximum of 192 months (16 years). Columns 3–4 indicate that the sample spans firms ranging from very small (market capitalization of \$700

⁷Prior to 2005, CDS coverage is limited, rendering the data less suitable for machine-learning applications.

⁸As documented by Liu (2022), XR contracts became the standard for U.S. corporates following the 2009 CDS Big Bang, whereas MR (modified restructuring) contracts were more common prior to that event. XR spreads primarily reflect default risk, while MR spreads reflect both default and restructuring risk.

million) to very large (market capitalization of \$1.73 trillion). Columns 5–6 show that firms cover a wide spectrum of credit quality, from AA-rated to CCC- and D-rated firms.⁹ These statistics highlight the broad coverage of the CDS market in terms of firm size, credit quality, and sample duration.

We use the logarithm of CDS spreads as the target variable. CDS spreads are strongly right-skewed, and commonly used loss functions in machine learning, such as the mean squared error (MSE), are highly sensitive to skewness: large observations receive disproportionate weight and can dominate the loss. As a result, a model trained on levels may overfit extreme observations at the expense of fitting the bulk of the distribution. To mitigate this issue, we apply a logarithmic transformation to CDS spreads and use the transformed variable as the target in our prediction model. Figure 3 presents the histogram of log CDS spreads. The mean log CDS spread is approximately -4.69 , with a standard deviation of 0.94 .

Node Characteristics. We construct 94 firm-level characteristics following [Gu, Kelly, and Xiu \(2020\)](#). Of these, 61 characteristics are updated annually, 13 quarterly, and 20 monthly. These characteristics are designed to capture distinct and largely nonredundant information about firm fundamentals.¹⁰

In addition, we include eight macroeconomic variables from [Welch and Goyal \(2008\)](#): the dividend-price ratio (dp), earnings-price ratio (ep), book-to-market ratio (bm), net equity issuance (ntis), Treasury-bill rate (tbl), term spread (tms), default spread (dfy), and stock variance (svar).¹¹ In total, we use 112 node-level features. Following [Kelly, Pruitt, and Su \(2019\)](#) and [Freyberger, Neuhierl, and Weber \(2020\)](#), all characteristics are rank-normalized cross-sectionally each month and mapped to the interval $[-1, 1]$.

Edge Characteristics. To construct edge-level features, we estimate pairwise idiosyncratic volatility spillovers using CRSP daily stock returns, consistent with the structural framework. This procedure follows [Chen \(2023\)](#), which generalizes the systemic risk measures developed in [Diebold and Yilmaz \(2014\)](#). We assume that firms within the same industry produce similar products and are subject to similar productivity-specific shocks. Accordingly, we estimate risk spillovers at the sector level and impose them on firms based on industry classification.

⁹The firm count exceeds 678 because some firms experience rating changes over time and are therefore associated with multiple ratings during the sample period. Sectoral distributions of CDS contracts are reported in Internet Appendix B.

¹⁰We account for data release delays following [Gu, Kelly, and Xiu \(2020\)](#) and [Gu, Kelly, and Xiu \(2021\)](#). The underlying data and replication codes for early years are provided by the authors. Related literature includes [Fama and French \(2016\)](#), [Green, Hand, and Zhang \(2017\)](#), [Hou, Xue, and Zhang \(2020\)](#), [Gu, Kelly, and Xiu \(2021\)](#), and [Kelly, Malamud, and Zhou \(2024\)](#). Details of all characteristics are provided in Internet Appendix C.

¹¹Including interactions between firm-level and macroeconomic variables yields similar out-of-sample results.

Specifically, we compute daily industry returns as value-weighted averages of firm returns. For each calendar month, we regress daily industry returns on the Fama–French three factors and treat the residuals as idiosyncratic industry returns.¹² Monthly idiosyncratic volatility is then computed as the standard deviation of daily idiosyncratic returns.

We estimate pairwise idiosyncratic volatility spillovers using a rolling-window LASSO vector autoregression (VAR). For each 90-month rolling window, we estimate a VAR for the panel of sector-level log idiosyncratic volatilities and perform a generalized variance decomposition (GVD) for 6-month-ahead forecast errors.¹³ This procedure yields a 48×48 matrix of spillover intensities, where each element a_{ij} measures the contribution of shocks originating in sector j to the idiosyncratic volatility of sector i . These measures constitute the empirical counterpart of the structural spillover weights a_{ij} in the model.

We collect the estimated a_{ij} from each rolling window to form a time-varying adjacency matrix A_t updated at a monthly frequency.¹⁴

Extrapolation to the Firm Level. After obtaining sector-level spillover measures, we extrapolate them to the firm level by imposing sectoral risk spillovers on firms according to their industry classifications. Figure 2 illustrates this procedure.

FIGURE 2 ABOUT HERE

Figure 2 shows an example with three sectors and five firms. If the spillover intensity from sector 2 to sector 1 equals 0.1, then this value is assigned as the spillover intensity from any firm in sector 2 to any firm in sector 1.

By imposing sector-level adjacency matrices at the firm level, we map inter-sectoral dependencies into inter-firm dependencies. This approach implicitly assumes that firms within the same sector are representative of sector-level production and risk exposure. While heterogeneity undoubtedly exists within industries, this assumption is consistent with our production-network framework, in which firms within a sector face similar productivity shocks. For clarity, we abstract from additional firm-specific shock channels.

Finally, one may ask why we do not construct idiosyncratic volatility spillovers directly from CDS data.

¹²Results are robust to removing only the CAPM factor, removing five principal components, or not removing common factors at all.

¹³Results are robust to rolling windows ranging from 80 to 100 months and forecast horizons between 6 and 10 months.

¹⁴The adjacency matrix at time t is constructed using data from $t - 90$ to t . Results are robust to lagging edge inputs by one month to avoid look-ahead bias. Prior work (e.g., Kryzanowski, Perrakis, and Zhong, 2017) finds that CDS markets tend to lead equity markets in response to negative news by days or weeks.

We do not pursue this approach because corporate CDS data exhibit substantial noise, sparse coverage, infrequent trading, and non-transaction-based quotes that vary significantly across time and firms. In contrast, equity market data are cleaner, higher frequency, and better suited for constructing reliable spillover measures. Moreover, using stock data aligns naturally with our structural framework, in which equity prices reflect firm value and default risk.

Training Configuration and Benchmark We construct a monthly panel in which the inputs consist of firm-level node characteristics and inter-firm edge characteristics, and the target variable is the CDS spread. As discussed above, we adopt a vanilla GNN architecture that operates primarily in the cross section. Accordingly, for each month t , we train the GNN using the full cross-sectional network observed at month t . We then use the $t + 1$ snapshot as a validation set to tune hyperparameters and prevent overfitting, and we generate out-of-sample predictions for month $t + 1$. For all GNN specifications, we use stochastic gradient descent (SGD) as the optimizer. To mitigate overfitting, we implement early stopping and select all hyperparameters by minimizing the mean squared error on the validation set.

We recursively refit the model each month to incorporate the most recent node-level and edge-level information, despite the associated computational cost, until the end of the sample period. This rolling training scheme ensures that all reported predictions are strictly out of sample.

To benchmark the performance of models that do not incorporate network edge information, we consider a set of alternative nonlinear machine-learning methods, including convolutional neural networks (CNN), gradient boosting regression trees (GBRT), random forests (RF), principal component regression (PCR), partial least squares (PLS), and support vector regression (SVR). These models use the same set of firm-level node characteristics as inputs but do not incorporate inter-firm edge features. All competing models are trained using the same rolling data partitions and evaluated under the same out-of-sample protocol as the GNN.

To provide a clean and internally consistent benchmark for the GNN, the CNN model is designed under strict architectural restrictions such that it is equivalent to a GNN with all network edges removed. Specifically, this benchmark preserves the same inter-layer and intra-layer structure as the GNN, but replaces the adjacency matrix with the identity matrix, effectively eliminating all cross-node message passing. The model uses the same number of layers, activation functions, and parameter-sharing structure as the GNN, and excludes any graph-level normalization. We hand-code the architecture to ensure that this zero-edge

GNN collapses exactly to a per-node feedforward network. For simplicity, we refer to this restricted model as CNN throughout the paper. Detailed descriptions of all comparison algorithms are provided in Internet Appendix D.

3.3 Empirical Results

We evaluate the importance of network edge features in explaining credit spreads by examining both pooled out-of-sample (OOS) performance across the entire sample and time-series variation in OOS performance. The OOS evaluation provides an objective assessment of predictive accuracy.

Pooled Out-of-Sample Performance. Table 2 reports pooled OOS performance for all machine-learning models. Panel A reports pooled out-of-sample root mean squared errors (RMSEs), while Figure 4 visualizes these results using bar plots.

TABLE 2 AND FIGURE 4 ABOUT HERE

Column 1 of Table 2 reports RMSEs for the full sample from March 2005 to December 2020. Columns 2 and 3 report RMSEs for investment-grade (BBB and above) and high-yield (BB and below) firms, respectively. Columns 4 and 5 report RMSEs for firms below and above the median market capitalization.

The results in Column 1 show that GNN models, across different architectural depths, achieve RMSEs of approximately 0.89—less than half of those produced by alternative algorithms. Under identical training conditions, CNN models exhibit substantially higher RMSE: 1.34 with two hidden layers. While increasing CNN depth initially improves performance, additional layers lead to deterioration, likely due to overfitting. In contrast, GNN performance is remarkably stable across architectures: even a single hidden layer is sufficient to capture the relevant network topology, and additional layers yield limited incremental gains. This stability reflects diminishing returns from repeated aggregation over a fixed network structure.

Tree-based methods (GBRT and RF) outperform dimension-reduction approaches (PCR and PLS) and support vector regression (SVR), but still underperform relative to CNNs and substantially underperform relative to GNNs. Overall, these results indicate that incorporating network topology—specifically inter-firm idiosyncratic risk spillovers—accounts for a substantial share of the cross-sectional variation in CDS spreads.

Columns 2 and 3 show that GNN models deliver substantial performance gains for both investment-grade and high-yield firms. For investment-grade firms, RMSEs from CNN2 are approximately 1.4, whereas GNN RMSEs are around 0.9. For high-yield firms, RMSEs from alternative models are approximately 1.2,

compared with about 0.85 for GNNs. These results indicate that network information improves predictive accuracy across credit qualities, with particularly pronounced gains for investment-grade firms. Intuitively, investment-grade firms tend to be larger, more central, and more interconnected within production and trade networks; as a result, their CDS spreads are especially sensitive to network-wide spillovers, which GNNs are well suited to capture.

Columns 4 and 5 show that GNN models outperform competing algorithms for both small and large firms. For small firms, RMSE declines from 1.30 (CNN2) to 0.80 (GNN2), while for large firms RMSE declines from 1.39 to 0.96. These improvements are of comparable magnitude. However, we note that firms in our sample are predominantly small to medium-sized, and therefore we refrain from drawing strong conclusions regarding size-based heterogeneity.

Economic Significance of Network Effects. To assess the economic magnitude of network effects, Panel B of Table 2 reports two additional measures.

The first measure is the *network-attributable spread change* (NSC), which captures the magnitude of the network-induced change in credit-spread levels relative to a node-only benchmark:

$$\text{NSC} \equiv \frac{\mathbb{E} \left[\left| \widehat{\log s}^{\text{GNN}} - \widehat{\log s}^{\text{CNN}} \right| \right]}{|\mathbb{E}[\log s]|}.$$

Here, $\widehat{\log s}^{\text{GNN}}$ denotes the predicted log CDS spread from GNN2, $\widehat{\log s}^{\text{CNN}}$ denotes the predicted log CDS spread from CNN2, and $\log s$ denotes the realized log CDS spread. The numerator measures the average magnitude of the network-induced *change* in the predicted log spread level when network information is incorporated, while the denominator normalizes this change by a typical log spread level. This normalization yields a scale-free statistic that facilitates comparison across samples, industries, and time.

NSC can be interpreted as an average treatment–style effect relative to a node-only baseline, quantifying how much the inclusion of network information shifts the level of predicted credit spreads. Panel B shows that incorporating network edge features induces an average spread change of approximately 21.8% in the full sample. The network-induced change is larger for high-yield firms (30.1%) than for investment-grade firms (18.5%), and larger for small firms (26.6%) than for large firms (17.7%).

In addition to NSC, we report an incremental explanatory-power measure, denoted Inc_R^2 :

$$Inc_R^2 \equiv 1 - \frac{\mathbb{E}\left[\left(\widehat{\log s}^{\text{GNN}} - \log s\right)^2\right]}{\mathbb{E}\left[\left(\widehat{\log s}^{\text{CNN}} - \log s\right)^2\right]}.$$

This statistic measures the fraction of node-only prediction error eliminated by incorporating network edge features.

As reported in Panel B, the average incremental R^2 is approximately 0.56, with particularly pronounced gains for investment-grade firms and for relatively smaller firms in our sample. Given the limited size coverage of our data, we refrain from drawing strong conclusions regarding size-related heterogeneity. Nevertheless, the results consistently indicate that network edge information is especially informative for explaining the credit spreads of investment-grade firms, which tend to be more central and embedded in complex trade and production relationships.

While network edge information also improves the prediction of credit spreads for high-yield firms, the associated gains in explanatory power are more modest than those observed for investment-grade firms. A plausible explanation is that high-yield firms are closer to default, and their credit risk is more strongly driven by firm-specific fundamentals and balance-sheet conditions. As a result, firm-level characteristics account for a larger proportion of the variation in their credit spreads, even though network information remains economically relevant.

Time-Series Variation in Out-of-Sample Performance. We next examine the time-series performance of network features. Figure 5 plots the monthly out-of-sample RMSEs for each algorithm.

FIGURE 5 ABOUT HERE

Figure 5 shows that GNN models consistently outperform all competing models over time. In certain periods, GNN RMSEs are as low as one-quarter of those produced by alternative algorithms, particularly relative to dimension-reduction methods such as PCR and PLS. This persistent outperformance highlights the importance of pairwise inter-firm network information in explaining CDS spreads.

More importantly, the time-series results reveal distinct episodes during which network structure becomes especially informative for CDS pricing. The first such episode coincides with the 2008 Global Financial Crisis. During periods of severe economic stress, production networks are disrupted as firms face binding

liquidity constraints, operational shutdowns, and heightened default risk. In this environment, inter-firm contagion and counterparty exposure become first-order determinants of credit spreads. As idiosyncratic shocks propagate through production and financial linkages, CDS spreads increasingly reflect network position rather than standalone firm fundamentals. GNNs are well suited to capture these contagion effects, whereas models that abstract from network structure perform poorly.

A second episode arises in late 2009 and early 2010, a transitional phase following the crisis. Although equity markets rebounded sharply during this period, production and counterparty networks remained impaired and were undergoing reconfiguration. Firms adjusted supplier relationships, renegotiated contracts, and reallocated production across newly constrained networks. This re-wiring process introduced substantial uncertainty that was not immediately reflected in balance-sheet or accounting data. As a result, models that rely solely on firm-level features exhibit a sharp deterioration in predictive performance. In contrast, GNNs continue to perform well by incorporating evolving inter-firm dependencies that shape downside credit risk during this network re-equilibration phase.

A third episode occurs around 2018, coinciding with the escalation of trade tensions and the introduction of tariff policies. From a network perspective, tariffs represent shocks to trade and production linkages that increase fragility within global value chains. Firms' exposure to affected suppliers and customers becomes a key determinant of credit risk, as disruptions propagate asymmetrically through the network. During this period, CDS spreads reflect not only firm-specific conditions but also indirect exposure to trade partners facing heightened uncertainty. The superior performance of GNNs during this episode underscores the role of network structure in transmitting trade-related shocks into credit markets.

Finally, following the onset of the COVID-19 pandemic in 2020, widespread production shutdowns generated severe upstream supply disruptions. The sudden closure of critical nodes—such as semiconductor manufacturing facilities—had cascading effects on downstream firms that depended on these inputs. Credit risk during this period was therefore shaped by firms' positions within disrupted supply chains rather than by their pre-pandemic fundamentals alone. GNNs effectively capture these cascading network effects, while non-network models struggle to account for the resulting comovement in CDS spreads.

Taken together, the time-series evidence not only supports the predictions of our structural framework but also highlights the state-dependent importance of inter-firm networks in credit markets. In periods of stress, transition, or structural disruption, the full network topology captures an economically meaningful component of systematic risk that is priced in CDS spreads. These findings are consistent with the production-network

literature (e.g., [Acemoglu et al., 2012](#)), which emphasizes that network structure provides a microfoundation for aggregate risk and its amplification.

To examine how global network features differentially affect sectors within the production network over time, we plot the network-attributable spread change (NSC) for firms across Fama–French 48 industries and across out-of-sample months.

Figure 6 presents a heatmap of the time-varying NSC across industries. For each month and each Fama–French 48 industry, we compute NSC as the average absolute difference between the predicted log CDS spread from GNN2 and that from CNN2, normalized by the average log CDS spread within the industry. At each month, industries are ranked by NSC. The five industries with the largest network-attributable spread change are highlighted in red, while the five industries with the smallest network-attributable spread change are highlighted in blue; all remaining industries are shown in white.

FIGURE 6 ABOUT HERE

As shown in Figure 6, several industries consistently appear among those with the highest NSC. These include Industry 22 (electrical equipment, covering electronic transmission and distribution equipment and electrical apparatus), Industry 25 (shipbuilding and railroad equipment), and Industry 26 (defense-related industries, including guided missiles and tanks).

In contrast, several industries consistently appear among those with the lowest NSC, including Industry 7 (entertainment, such as film and live performances), Industry 15 (rubber and plastic products), Industry 16 (textiles, including textile mill and canvas products), Industry 28 (mining, including metal and nonmetallic mining), and Industry 29 (coal, including bituminous coal and lignite mining).

These patterns are economically intuitive. Network features tend to matter more for firms that (i) occupy intermediate positions in the production chain and are exposed to both upstream and downstream risks, (ii) rely heavily on shipping, logistics, and distribution across the supply chain, or (iii) depend on specialized inputs that are difficult to substitute. For such firms, disruptions or shocks propagating through supplier–customer relationships can lead to substantial changes in expected cash flows and, consequently, credit spreads.

The industries highlighted in red—notably electrical equipment, shipbuilding, railroad equipment, and defense—are precisely those that lie at critical intermediate nodes of the production and trade network. Their

revenues depend on continuous flows from multiple counterparties, making them particularly sensitive to network-level disruptions. Defense-related firms, in particular, rely on highly specialized and sophisticated components sourced through rigid supply chains and often operate under long-term contracts. This network rigidity, characterized by low input substitutability, amplifies the importance of network edge information in determining the credit health of the defense sector. Consistent with this interpretation, network features induce especially large spread changes for defense sector during the period from 2014 to 2018, which coincides with discrete geopolitical shocks such as the Russia–Ukraine conflict and conflicts involving ISIS. During such periods, defense demand becomes lumpy and state-dependent, and contracts may be renegotiated, accelerated, delayed, or repriced.

By contrast, the industries highlighted in blue are those whose credit risk is primarily driven by firm-specific fundamentals or final demand. For example, firms in natural resource extraction (mining and coal) are heavily influenced by commodity prices and balance-sheet leverage, which dominate network considerations. Similarly, entertainment and textile firms rely more heavily on idiosyncratic fundamentals such as intellectual property, brand value, and consumer sentiment, and often operate with more diversified supplier and customer bases. As a result, network edge features induce relatively smaller shifts in their credit spreads.

4 Conclusion

This paper develops a structural framework for credit counterparty risk in which idiosyncratic shocks propagate through an inter-firm production network. By explicitly modeling firms’ economic linkages as input–output relationships, the framework clarifies how both a firm’s position within the network and the global network topology shape the transmission of idiosyncratic default risk and the cross-sectional behavior of credit spreads. The model allows for asymmetric contagion, cascading effects, and ordinary firm-specific shocks, and links production-network spillovers to default intensities and CDS spreads through a distance-to-default channel.

To provide empirical support for the structural mechanism, we propose a parsimonious network-based empirical approach that directly incorporates the full inter-firm network topology. Using graph neural networks (GNNs), we embed both firm-level characteristics and pairwise idiosyncratic risk spillovers into a unified prediction framework. This approach overcomes a key limitation of standard empirical and machine-

learning methods, which typically rely on firm-level features and cannot incorporate the entire $n \times n$ network structure as a predictive object.

Empirically, we find that models incorporating production-network information substantially outperform non-network benchmarks in predicting CDS spreads. The improvement is economically large, persistent across firm size and credit quality, and particularly pronounced during periods of financial stress, economic transitions, and supply-chain disruptions. These findings indicate that inter-firm network structure captures an important component of credit risk that is not explained by firm fundamentals or common shocks alone, and that this network-based risk is state-dependent and priced in CDS markets.

Overall, our results provide direct empirical support for a production-network-based view of counterparty risk. They suggest that credit spreads reflect not only firms' standalone default risk, but also their exposure to idiosyncratic shocks originating elsewhere in the network. More broadly, the paper demonstrates how combining structural economic modeling with modern network-based machine-learning tools can yield new insights into credit risk, contagion, and systemic risk. An important direction for future research is to extend the framework to incorporate other forms of inter-firm linkages—such as financial exposures or dealer networks—and to study the dynamic evolution of network risk over time.

Table 1. Summary Statistics of CDS Contracts and Issuing Firms

This table presents summary statistics for CDS contracts and their issuing firms from January 2005 to December 2020. Columns 1-2 show CDS contract duration statistics. Columns 3-4 show firms' market capitalization statistics. Columns 5-6 present the distribution of firms' credit ratings.

CDS Duration		Firm Market Capitalization		Firm Rating Distribution	
	Month		Dollar(\$)	Rating	Firm Count
mean	117	mean	2.65×10^7	AA	97
std	69	std	5.38×10^7	A	144
min	2	min	7.01×10^2	BBB	192
25%	50	25%	3.57×10^6	BB	156
50%	137	50%	1.01×10^7	B	88
75%	188	75%	2.64×10^7	CCC	59
max	192	max	1.71×10^9	D	3

Table 2. Out-of-Sample Performance and Network Attribution. Panel A reports pooled out-of-sample root mean squared errors (RMSEs) for alternative machine-learning models. Panel B reports the economic contribution of network edge information beyond node characteristics, measured by the network-attributable spread change (NSC) and the incremental R^2 (Inc_ R^2). Column 1 reports the full sample (March 2005–December 2020). Columns 2–3 report investment-grade (BBB and above) and high-yield (BB and below) firms. Columns 4–5 report small (below-median market capitalization) and large (at or above median market capitalization) firms. NSC is defined as $\mathbb{E}[|\widehat{\log s}^{\text{GNN}} - \widehat{\log s}^{\text{CNN}}|]/|\mathbb{E}[\log s]|$. Inc_ R^2 is defined as $1 - \text{MSE}_{\text{GNN}}/\text{MSE}_{\text{CNN}}$. Predicted log spreads are obtained from CNN2 and GNN2.

	All	Investment Grade	High Yield	Small	Big
Panel A: Pooled Out-of-Sample RMSE					
RF	1.665	1.828	1.271	1.464	1.845
GBRT	1.900	2.128	1.320	1.570	2.181
PCR	2.196	2.527	1.283	1.501	2.719
PLS	2.348	2.679	1.459	1.679	2.865
SVR	1.876	2.103	1.296	1.540	2.160
CNN1	2.245	2.308	2.110	2.072	2.405
CNN2	1.338	1.392	1.221	1.282	1.391
CNN3	1.378	1.437	1.249	1.337	1.418
GNN1	0.890	0.909	0.850	0.808	0.965
GNN2	0.888	0.904	0.854	0.809	0.960
GNN3	0.893	0.915	0.847	0.808	0.972
Panel B: Network-Attributable Spread Change and Incremental R^2					
NSC	0.218	0.185	0.301	0.266	0.177
Inc_ R^2	0.560	0.578	0.511	0.602	0.524

Figure 1. Inter-Layer Design of the GNN

This figure depicts the inter-layer message-passing architecture of the GNN algorithm, where node embeddings are generated according to the GCN procedure proposed in [Kipf and Welling \(2016\)](#).

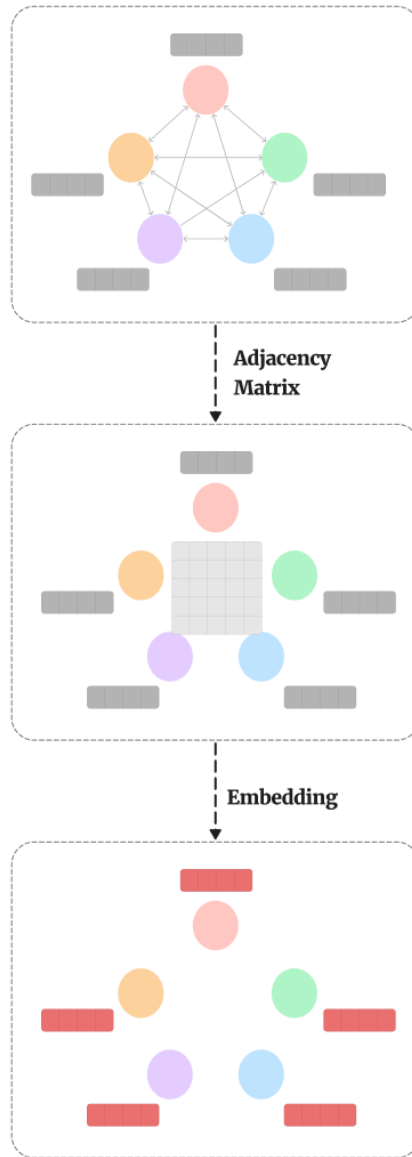
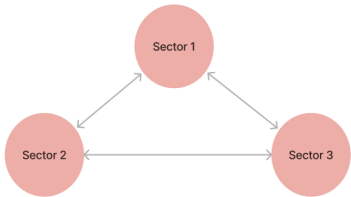


Figure 2. Extrapolation of Sector-Level Network Effects to Firm Level

This figure illustrates the process of extrapolating sector-level idiosyncratic risk spillover to the firm level. Panel A depicts risk spillover among three sectors, estimated from the Generalized Variance Decomposition (GVD) of VAR forecast errors. In the adjacency matrix, element (i,j) indicates the risk spillover intensity from sector j to sector i . Panel B demonstrates the extrapolation of this risk spillover to five firms across the three sectors.

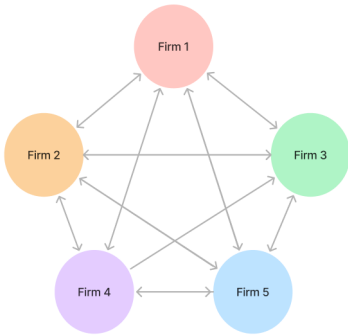
Panel A: Example for risk spillover among 3 sectors



	Sector 1	Sector 2	Sector 3
Sector 1	0.4	0.1	0.5
Sector 2	0.25	0.6	0.15
Sector 3	0.25	0.45	0.3

Panel B: Example for extrapolation

Firm	Sector 1	Sector 2	Sector 3
Firm 1	1	0	0
Firm 2	0	1	0
Firm 3	1	0	0
Firm 4	0	0	1
Firm 5	0	1	0



	Firm 1	Firm 2	Firm 3	Firm 4	Firm 5
Firm 1	0.4	0.1	0.4	0.5	0.1
Firm 2	0.25	0.6	0.25	0.15	0.6
Firm 3	0.4	0.1	0.4	0.5	0.1
Firm 4	0.25	0.45	0.25	0.3	0.45
Firm 5	0.25	0.6	0.25	0.15	0.6

Figure 3. Distribution of Log CDS Spreads

This figure displays the histogram of log CDS spreads for 5-year tenor, senior unsecured contracts from January 2005 to December 2020.

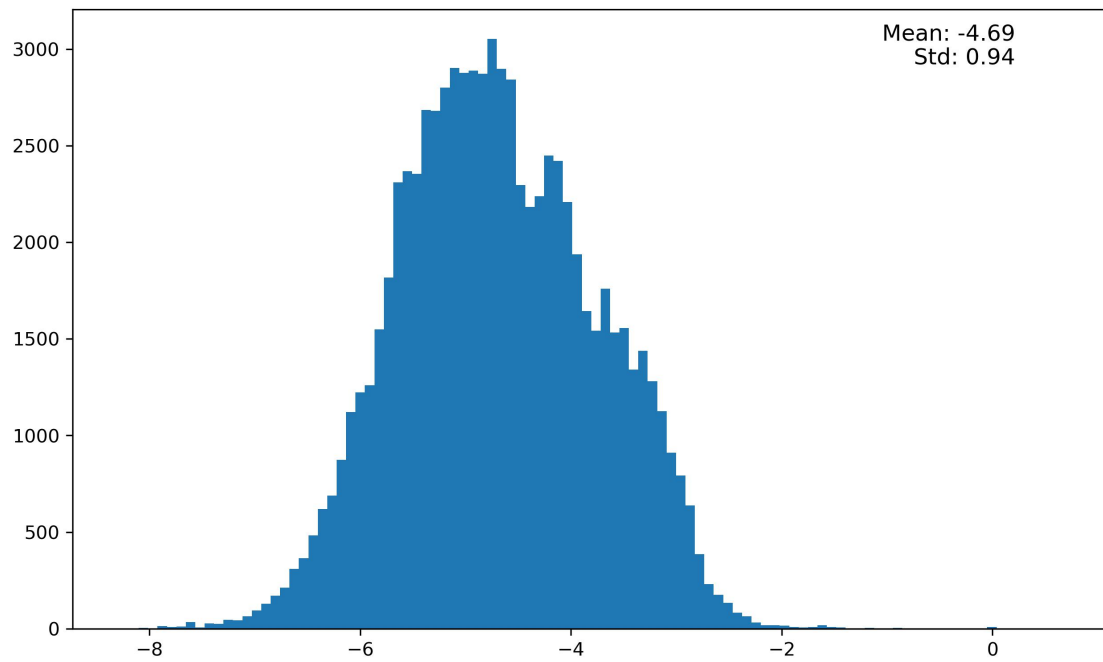
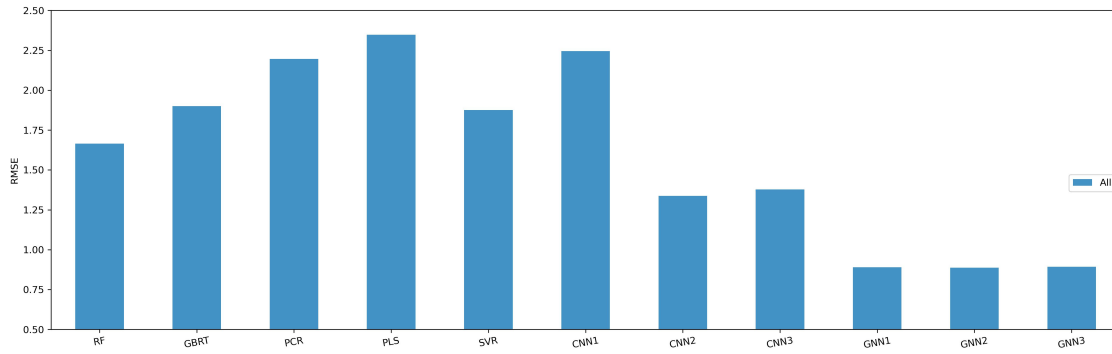
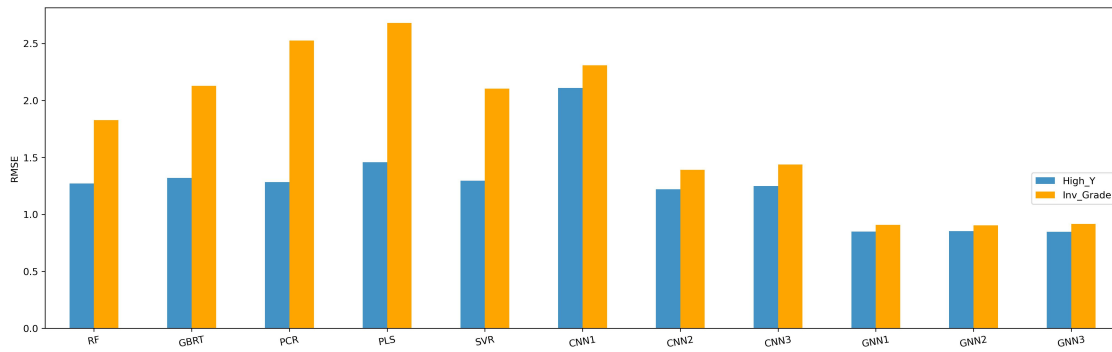


Figure 4. Out-of-Sample Prediction Error of Machine Learning Algorithms

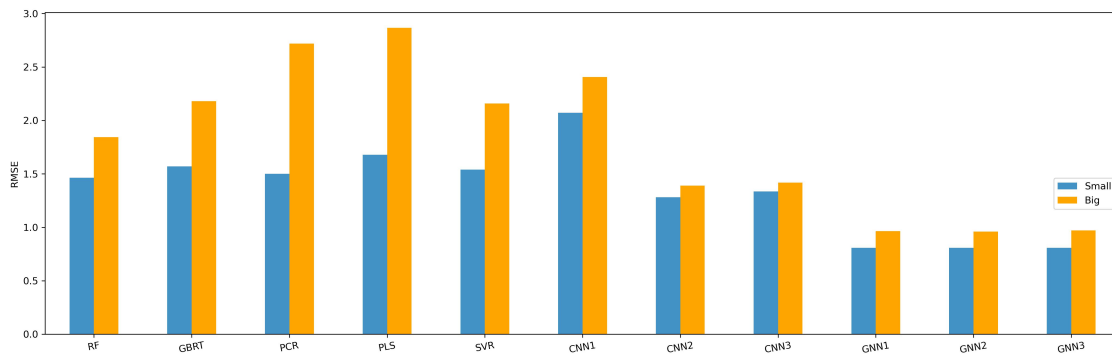
This figure presents the out-of-sample prediction error of various machine learning algorithms using pooled Root Mean Square Error (RMSE). Panel A displays the overall RMSE across all out-of-sample periods. Panel B presents the overall RMSE by firm credit rating, with investment grade defined as BBB or above and high-yield as BB or below. Panel C shows the overall RMSE by firm size, with small firms defined as those below the median market capitalization and large firms as those at or above the median.



(a) Pooled RMSE



(b) Pooled RMSE by Firm Credit Rating



(c) Pooled RMSE by Firm Market Capitalization

Figure 5. Time Series of Out-of-Sample Prediction Error. This figure plots the monthly out-of-sample root mean squared error (RMSE) for all machine-learning algorithms over the period from March 2015 to December 2020.

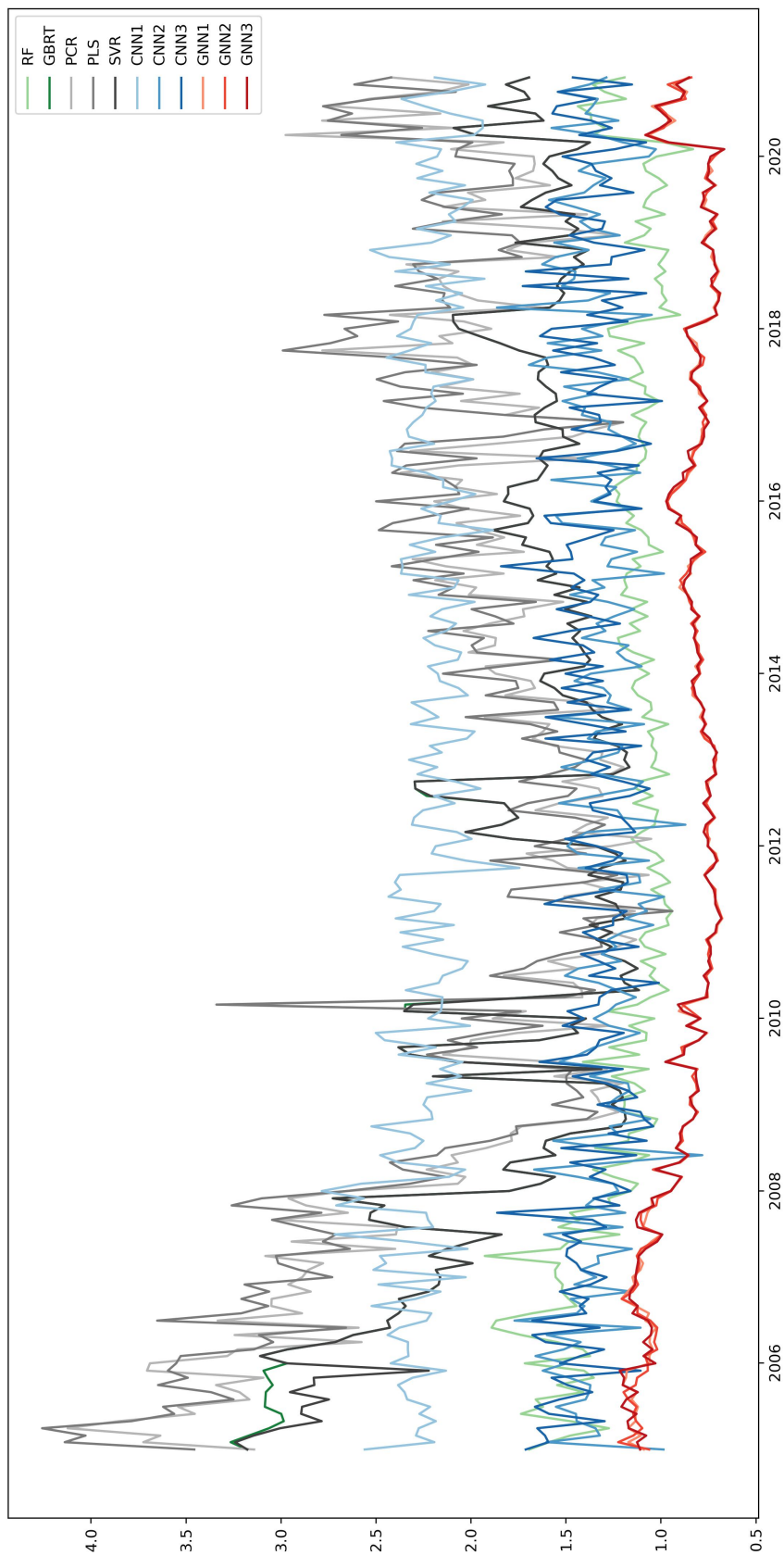
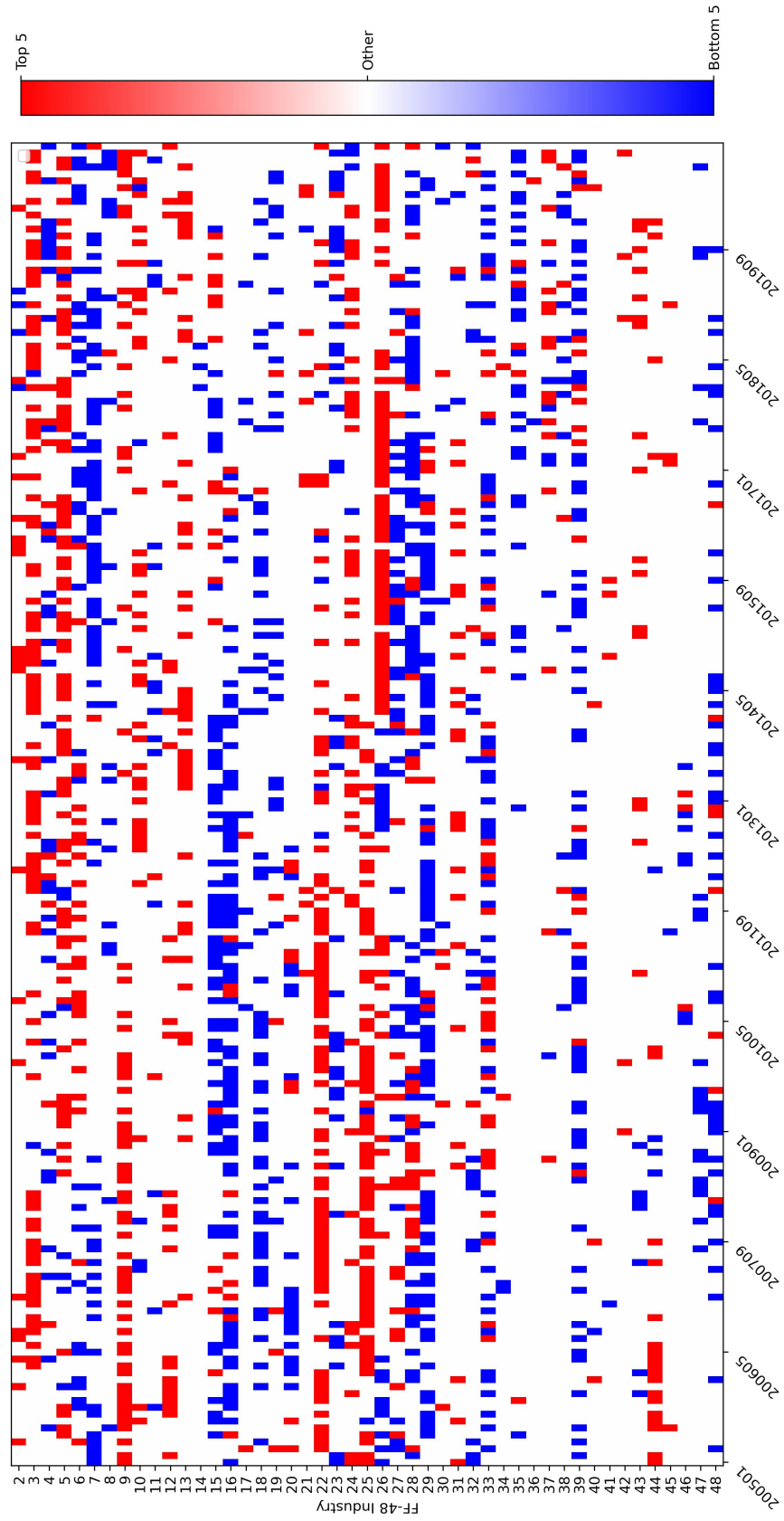


Figure 6. Time-Varying Network-Attributable Spread Changes Across Industries. This figure presents a heatmap of the time-varying network-attributable spread change (NSC) across industries. For each month and each Fama–French 48 industry, we compute NSC, defined as the average absolute difference between the predicted log CDS spread from GNN2 and that from CNN2, normalized by the average log CDS spread within the industry. At each month, industries are ranked by NSC. The five industries with the largest network-attributable spread change (NSC) are highlighted in red, while the five industries with the smallest network-attributable spread change are highlighted in blue; all remaining industries are shown in white.



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